A Bibliography of Publications by, and about, Magnus Rudolph Hestenes

Nelson H. F. Beebe
University of Utah
Department of Mathematics, 110 LCB
155 S 1400 E RM 233
Salt Lake City, UT 84112-0090
USA

Tel: +1 801 581 5254

E-mail: beebe@math.utah.edu, beebe@acm.org, beebe@computer.org (Internet)
WWW URL: https://www.math.utah.edu/~beebe/

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Abstract

This bibliography records publications of Magnus Rudolph Hestenes.

Title word cross-reference

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